up and down in perfect synchronization, while a coefficient of -1.0 means the variables always move in opposite directions. A correlation coefficient of zero suggests that the two variables are not related to one another; that is, they are independent.

j. Market risk is that part of a security’s total risk that cannot be eliminated by diversification. It is measured by the beta coefficient. Diversifiable risk is also known as company specific risk, that part of a security’s total risk associated with random events not affecting the market as a whole. This risk can be eliminated by proper diversification. The relevant risk of a stock is its contribution to the riskiness of a well-diversified portfolio.

k. The beta coefficient is a measure of a stock’s market risk, or the extent to which the returns on a given stock move with the stock market. The average stock’s beta would move on average with the market so it would have a beta of 1.0.

l. The security market line (SML) represents in a graphical form, the relationship between the risk of an asset as measured by its beta and the required rates of return for individual securities. The SML equation is essentially the CAPM: $r_i = r_f + \beta_i(r_m - r_f)$.

m. The slope of the SML equation is $(r_m - r_f)$, the market risk premium. The slope of the SML reflects the degree of risk aversion in the economy. The greater the average investors aversion to risk, then the steeper the slope, the higher the risk premium for all stocks, and the higher the required return.

2-2 a. The probability distribution for complete certainty is a vertical line.

b. The probability distribution for total uncertainty is the X axis from $-\infty$ to $+\infty$.

2-3 Security A is less risky if held in a diversified portfolio because of its lower beta and negative correlation with other stocks. In a single-asset portfolio, Security A would be more risky because $\sigma_A > \sigma_B$ and $CVA > CV_B$.

2-4 a. No, it is not riskless. The portfolio would be free of default risk and liquidity risk, but inflation could erode the portfolio’s purchasing power. If the actual inflation rate is greater than the expected, interest rates in general will rise to incorporate a larger inflation premium (IP) and the value of the portfolio would decline.

b. No, you would be subject to reinvestment rate risk. You might expect to “roll over” the Treasury bills at a constant (or even increasing) rate of interest, but if interest rates fall, your investment income will decrease.

Answers and Solutions: 2-8
c. A U.S. government-backed bond that provided interest with constant purchasing power (that is, an indexed bond) would be close to riskless.

2-5  a. The expected return on a life insurance policy is calculated just as for a common stock. Each outcome is multiplied by its probability of occurrence, and then these products are summed. For example, suppose a 1-year term policy pays $10,000 at death, and the probability of the policyholder’s death in that year is 2 percent. Then, there is a 98 percent probability of zero return and a 2 percent probability of $10,000:

\[
\text{Expected return} = 0.98(0) + 0.02(10,000) = 200.
\]

This expected return could be compared to the premium paid. Generally, the premium will be larger because of sales and administrative costs, and insurance company profits, indicating a negative expected rate of return on the investment in the policy.

b. There is a perfect negative correlation between the returns on the life insurance policy and the returns on the policyholder’s human capital. In fact, these events (death and future lifetime earnings capacity) are mutually exclusive.

c. People are generally risk averse. Therefore, they are willing to pay a premium to decrease the uncertainty of their future cash flows. A life insurance policy guarantees an income (the face value of the policy) to the policyholder’s beneficiaries when the policyholder’s future earnings capacity drops to zero.

2-6 The risk premium on a high beta stock would increase more.

\[
\text{RP}_j = \text{Risk Premium for Stock } j = (k_d - k_f)b.
\]

If risk aversion increases, the slope of the SML will increase, and so will the market risk premium \((k_m - k_f)\). The product \((k_d - k_f)b\) is the risk premium of the jth stock. If \(b\) is low (say, 0.5), then the product will be small; \(\text{RP}_j\) will increase by only half the increase in \(k_m\). However, if \(b\) is large (say, 2.0), then its risk premium will rise by twice the increase in \(k_m\).
According to the Security Market Line (SML) equation, an increase in beta will increase a company's expected return by an amount equal to the market risk premium times the change in beta. For example, assume that the risk-free rate is 6 percent, and the market risk premium is 5 percent. If the company's beta doubles from 0.8 to 1.6 its expected return increases from 10 percent to 14 percent. Therefore, in general, a company's expected return will not double when its beta doubles.

Yes, if the portfolio's beta is equal to zero. In practice, however, it may be impossible to find individual stocks that have a nonpositive beta. In this case it would also be impossible to have a stock portfolio with a zero beta. Even if such a portfolio could be constructed, investors would probably be better off just purchasing Treasury bills, or other zero beta investments.
SOLUTIONS TO END-OF-CHAPTER PROBLEMS

2-1 \[ \hat{r} = (0.1)(-50\%) + (0.2)(-3\%) + (0.4)(16\%) + (0.2)(25\%) + (0.1)(60\%) = 11.40\%. \]
\[ \sigma^2 = [(-50\% - 11.40\%)^2(0.1) + (-3\% - 11.40\%)^2(0.2) + (16\% - 11.40\%)^2(0.4) + (25\% - 11.40\%)^2(0.2) + (60\% - 11.40\%)^2(0.1)] = 712.44; \sigma = 26.69\%. \]
\[ CV = \frac{26.69\%}{11.40\%} = 2.34. \]

2-2

<table>
<thead>
<tr>
<th>Investment</th>
<th>Beta</th>
</tr>
</thead>
<tbody>
<tr>
<td>$35,000</td>
<td>0.8</td>
</tr>
<tr>
<td>$40,000</td>
<td>1.4</td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td><strong>$75,000</strong></td>
</tr>
</tbody>
</table>

\[ (\frac{35,000}{75,000})(0.8) + (\frac{40,000}{75,000})(1.4) = 1.12. \]

2-3 \[ k_{mf} = 5\%; R_D = 6\%; k_M = ? \]
\[ k_M = 5\% + (6\%-11\%) = 0\%. \]
\[ k_s, \text{ when } b = 1.2 = ? \]
\[ k_s = 5\% + 6\%(1.2) = 12.2\%. \]

2-4 \[ k_{fr} = 6\%; k_M = 13\%; b = 0.7; k_s = ? \]
\[ k_s = k_{fr} + (k_M - k_{fr})b = 6\% + (13\% - 6\%)0.7 = 10.9\%. \]

2-5 a. \[ \hat{r} = (0.3)(15\%) + (0.4)(9\%) + (0.3)(18\%) = 13.5\%. \]
\[ \hat{r}_D = (0.3)(20\%) + (0.4)(15\%) + (0.3)(12\%) = 11.6\%. \]

\[ \sigma_D = \sqrt{(0.3)(15\% - 13.5\%)^2 + (0.4)(9\% - 13.5\%)^2 + (0.3)(18\% - 13.5\%)^2} = 3.85\%. \]
\[ \sigma = \sqrt{(0.3)(20\% - 11.6\%)^2 + (0.4)(15\% - 11.6\%)^2 + (0.3)(12\% - 11.6\%)^2} = 6.22\%. \]

Answers and Solutions: 2 - 11
c. \( CV_m = \frac{3.85\%}{13.3\%} = 0.29 \).
\( CV_d = \frac{6.22\%}{11.4\%} = 0.54 \).

2-6

a. \( \bar{k} = \sum \frac{k_i}{n} \).

\( \bar{k}_x = 0.1(-35\%) + 0.2(0\%) + 0.4(20\%) + 0.2(25\%) + 0.1(45\%) \)
\( = 14\% \text{ versus } 12\% \text{ for } X. \)

b. \( \sigma = \sqrt{\sum \frac{(k_i - \bar{k})^2}{n}} \).

\( \sigma_x = (-10\% - 12\%)^2(0.1) + (2\% - 12\%)^2(0.2) + (12\% - 12\%)^2(0.4) \)
\( + (20\% - 12\%)^2(0.2) + (30\% - 12\%)^2(0.1) = 148.8\% \).

\( \sigma_Y = 12.20\% \text{ versus } 20.35\% \text{ for } Y. \)

\( CV_x = \frac{\sigma_x}{\bar{k}_x} = 12.20\%/14\% = 0.87, \text{ while } \)

\( CV_Y = 20.35\%/14\% = 1.45. \)

If Stock Y is less highly correlated with the market than X, then it
might have a lower beta than Stock X, and hence be less risky in a
portfolio sense.

2-7

a. \( k_a = k_{sy} + (k_m - k_{sy})b_a \),

\( 12\% = 5\% + (10\% - 5\%)b_a \)
\( 12\% = 5\% + 5\%(b_a) \)
\( 7\% = 5\%(b_a) \)
\( 1.4 = b_a. \)

b. \( k_a = 5\% + 5\%(b_a) \)
\( k_a = 5\% + 5\%(2) \)
\( k_a = 15\%. \)

2-8

a. \( k_d = k_{sy} + (k_m - k_{sy})b_d = 9\% + (14\% - 9\%)1.3 = 15.5\%. \)

b. 1. \( k_{sy} \) increases to 10%:

\( k_a \) increases by 1 percentage point, from 14\% to 15%.

\( k_d = k_{sy} + (k_m - k_{sy})b_d = 10\% + (15\% - 10\%)1.3 = 16.5\%. \)

Answers and Solutions: 2-12
2. **k_R decreases to 8%:**

   \[ k_R \] decreases by 1%, from 14% to 13%.

   \[ k_1 = k_{RF} + (k_R - k_{RF})b_1 = 8\% + (13\% - 8\%)1.3 = 14.5\%. \]

3. **1. k_R increases to 16%:**

   \[ k_1 = k_{RF} + (k_R - k_{RF})b_1 = 8\% + (16\% - 8\%)1.3 = 18.1\%. \]

4. **2. k_R decreases to 13%:**

   \[ k_1 = k_{RF} + (k_R - k_{RF})b_1 = 8\% + (13\% - 9\%)1.3 = 14.2\%. \]

**2-9 Old portfolio beta = \$142,500 \div \$150,000 (b) + \$7,500 \div \$150,000 (1.00) \]

1.12 = 0.95b + 0.05

1.07 = 0.95b

1.13 = b.

**New portfolio beta = 0.95(1.13) + 0.05(1.75) = 1.16.**

**Alternative Solutions:**

1. **Old portfolio beta = 1.12 = (0.05)b_1 + (0.05)b_2 + ... + (0.05)b_20**

   \[ \Sigma b_i = 1.12/0.05 = 22.4. \]

   **New portfolio beta = (22.4 - 1.0 + 1.75)(0.05) = 1.1575 = 1.16.**

2. **\Sigma b_i excluding the stock with the beta equal to 1.0 is 22.4 - 1.0 = 21.4, so the beta of the portfolio excluding this stock is b = 21.4/19 = 1.1263. The beta of the new portfolio is:**

   \[ 1.1263(0.95) + 1.75(0.05) - 1.1575 = 1.16. \]

**2-10 Portfolio beta = \$600,000 \div \$4,000,000 (1.50) + \$600,000 \div \$4,000,000 (-0.50) \]

\[ + \$1,000,000 \div \$4,000,000 (1.25) + \$2,000,000 \div \$4,000,000 (0.75) \]

\[ = 0.1(1.5) + 0.15(-0.50) + 0.25(1.25) + 0.5(0.75) \]

\[ = 0.15 - 0.075 + 0.3125 + 0.375 = 0.7625. \]

\[ k_R = k_{RF} + (k_R - k_{RF})b_R = 8\% + (14\% - 8\%)0.7625 = 12.1\%. \]
Alternative solution: First compute the return for each stock using the CAPM equation \(k_t = (k_G - k_M)b_t\), and then compute the weighted average of these returns.

\[
k_M = 6\% \text{ and } k_G - k_M = 8\%.
\]

<table>
<thead>
<tr>
<th>Stock</th>
<th>Investment</th>
<th>Beta</th>
<th>(k = k_M + (k_G - k_M)b_t)</th>
<th>Weight</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>$400,000</td>
<td>1.50</td>
<td>18%</td>
<td>0.10</td>
</tr>
<tr>
<td>B</td>
<td>$600,000</td>
<td>(0.50)</td>
<td>2</td>
<td>0.15</td>
</tr>
<tr>
<td>C</td>
<td>$1,000,000</td>
<td>1.25</td>
<td>16</td>
<td>0.25</td>
</tr>
<tr>
<td>D</td>
<td>$2,000,000</td>
<td>0.75</td>
<td>12</td>
<td>0.50</td>
</tr>
<tr>
<td>Total</td>
<td>$4,000,000</td>
<td></td>
<td></td>
<td>1.00</td>
</tr>
</tbody>
</table>

\[
k_p = 10\%(0.10) + 2\%(0.15) + 16\%(0.25) + 12\%(0.50) = 12.1\%.
\]

2-11 First, calculate the beta of what remains after selling the stock:

\[
b_p = \frac{1.1 = \frac{\$100,000}{\$2,000,000}}{0.9 + \frac{\$1,900,000}{\$2,000,000}b_A} = 1.1005.
\]

\[
b_A = \frac{(0.95)1.1005 + (0.05)1.4}{1.25} = 1.125.
\]

2-12 We know that \(b_A = 1.50\), \(b_B = 0.75\), \(k_M = 13\%\), \(k_G = 7\%\).

\[
k_I = k_M + (k_G - k_M)b_I = 13\% + 7\%b_I.
\]

\[
k_r = 7\% + 6\%(1.50) = 16.0\%
\]

\[
k_s = 7\% + 6\%(0.75) = 11.5\%.
\]

2-13 a. \($1 million \times 0.5\) + \($500,000 \times 0.5\) = \$0.5 million.

b. You would probably take the sure \$0.5 million.

c. Risk averter.

d. 1. \($1.15 million \times 0.5\) + \($500,000 \times 0.5\) = \$575,000, or an expected profit of \$75,000.

2. \$75,000/\$500,000 = 15\%.

3. This depends on the individual's degree of risk aversion.

4. Again, this depends on the individual.

Answers and Solutions: 2-14
5. The situation would be unchanged if the stocks' returns were perfectly positively correlated. Otherwise, the stock portfolio would have the same expected return as the single stock (15%) but a lower standard deviation. If the correlation coefficient between each pair of stocks was a negative one, the portfolio would be virtually riskless. Since \( r \) for stocks is generally in the range of 0.6 to 0.7, investing in a portfolio of stocks would definitely be an improvement over investing in the single stock.

2-14 a. \( \hat{r}_n = 0.1(7\%) + 0.2(9\%) + 0.4(11\%) + 0.2(13\%) + 0.1(15\%) = 11\% \).

\( k_M = 6\% \). (given)

Therefore, the SML equation is

\[ k_i = k_M + (k_M - k_R)b_i = 6\% + (11\% - 6\%)b_i = 6\% + (5\%)b_i. \]

b. First, determine the fund's beta, \( b_f \). The weights are the percentage of funds invested in each stock.

\[\begin{align*}
A &= \frac{160}{8500} = 0.19 \\
B &= \frac{122}{8500} = 0.016 \\
C &= \frac{680}{8500} = 0.081 \\
D &= \frac{890}{8500} = 0.105 \\
E &= \frac{680}{8500} = 0.081 \\
\end{align*}\]

\[\begin{align*}
b_f &= 0.32(0.5) + 0.24(2.0) + 0.16(4.0) + 0.16(1.0) + 0.12(3.0) \\
&= 0.16 + 0.48 + 0.64 + 0.16 + 0.36 = 1.8. \\
\end{align*}\]

Next, use \( b_f = 1.8 \) in the SML determined in Part a:

\[ k_i = 6\% + (11\% - 6\%)1.8 = 6\% + 9\% = 15\%. \]

c. \( k_R \) - Required rate of return on new stock = 6\% + (5\%)2.0 = 16\%.

An expected return of 15 percent on the new stock is below the 16 percent required rate of return on an investment with a risk of \( b = 2.0 \). Since \( k_R = 16\% > k_M = 15\% \), the new stock should not be purchased. The expected rate of return that would make the fund indifferent to purchasing the stock is 16 percent.